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ARTICLE

## Resolving origin of the multimode Jahn-Teller effect in metallophthalocyanines

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A detailed Density Functional Theory (DFT) analysis was performed in order to study the multimode Jahn-Teller (JT) problem in the electronic ground state of manganese phthalocyanine (MnPc). Comparison with magnesium phthalocyanine ion (MgPc<sup>-</sup>) and phthalocyanine trianion (Pc<sup>3-</sup>), also prone to the JT effect, is presented. Our results clarify the origin and provide the microscopic insight into the symmetry breaking process. The JT distortion is highly influenced by the coordination of phthalocyanine to the Mn<sup>II</sup> ion, and occurs over the whole system, while MgPc<sup>-</sup> complex ion possesses mainly ligand-based instability.

### Introduction

Phthalocyanines, structurally close to biologically relevant porphyrins, are molecules of the utmost importance in nanoelectronics,<sup>1</sup> optoelectronics,<sup>2</sup> chemical sensors,<sup>3</sup> and so forth. Although the first phthalocyanine was synthesized more than a century ago,<sup>4</sup> the development of new functional phthalocyanines is still relentlessly growing, due to their unique properties<sup>5</sup> and various potential uses in the modern science. Coordination to a metal ion leads to a great diversity of possibilities in the technological application, *e.g.* they are richly utilized as dyes<sup>6</sup> and catalysts<sup>7</sup>. Profound investigations indicate that atomically thin films of transition metal (TM) (copper, nickel, cobalt, iron, manganese) phthalocyanines, initially insulators, can become conductors through potassium doping, opening the way to a new class of superconductors.<sup>8,9</sup> Manganese phthalocyanine (MnPc) belongs to the class of organic semiconductors and molecular magnets.<sup>10</sup> MnPc acts as a spin-filter and its spin can be controlled in the defined manner,<sup>11-14</sup> presenting an important prerequisite for the possible use in molecular spintronics and quantum computing.<sup>15-18</sup> Therefore, metallophthalocyanines are deservedly called "the compounds of the 21st century".<sup>19</sup> Many ideas, questions and concerns related to the practical applications of this class of compounds require a quantitative

understanding of the chemistry and physics on the microscopic level.

Since 3d TM ion complexes in different spin states usually display quite different structural, spectral and magnetic properties, and also reactivity, it is important to correctly determine the spin ground state of the system. For instance, Mn<sup>II</sup> in MnPc has five d-electrons that can be distributed in a square-planar environment in three different ways: with a maximum number of unpaired electrons, leading to the high spin state, with maximally paired electrons – resulting in the low spin state, or intermediate spin. It was found that intermediate spin is the ground state,<sup>20</sup> however, different ground electronic states within this spin multiplicity are still a subject of debate in the literature.<sup>21-27</sup> In order to clarify these issues we performed Density Functional Theory (DFT) calculations with various Density Functional Approximations (DFAs) reliable for the spin state energetics. Furthermore, one of the possible, already reported, lowest-lying states, <sup>4</sup>E<sub>g</sub>, is the subject to the Jahn-Teller (JT) distortion.<sup>28,29</sup> To the best of our knowledge, the JT effect in MnPc was not analyzed so far, even the significance of the JT distortion and its influence on the properties of the systems is well recognized.<sup>29</sup> The distortion can be the inherent feature of the central metal ion in TM compounds, but may also originate from the ligand itself. Therefore, the comparison between 3s-metallophthalocyanine, magnesium phthalocyanine ion (MgPc<sup>-</sup>), and 3d-metallophthalocyanine, MnPc, can give answers on the nature of the distortion. Furthermore, the question is what happens with phthalocyanine trianion (Pc<sup>3-</sup>) that itself is an example of multimode  $E \otimes (b_1 + b_2)$  JT problem, the same as aforementioned complexes. For this purpose we performed DFT approach, developed by Daul *et al.*,<sup>30,31</sup> proven to be accurate for the analysis of the JT effect in medium-to-large molecules.<sup>32-36</sup> In addition, energy decomposition analysis

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(EDA),<sup>37</sup> the powerful tool for generating a compact, qualitative and quantitative picture of a chemical bond formation between the ligand and central metal ion,<sup>38</sup> was performed to afford microscopic insight into the macroscopic features. In this way we can explore different energy contributions and provide information about the changes that occur after the chemical bond is formed enabling us to understand how the central metal ion influences the distortion in these molecules, and hence how electronic structure control the nuclear motion in similar systems. In order to tackle the multimode problem and quantify the role played by different normal modes in symmetry breaking processes, the Intrinsic Distortion Path (IDP) model is employed.<sup>31-33,39,40</sup> The essence of the IDP model is to analyze multimode JT effect within harmonic approximation and to provide important chemical information like an approximation to the minimum energy path, and quantification of the forces along each JT active mode, or in other words calculation of the vibronic coupling constants.

### Computational details

The DFT calculations have been carried out using the Amsterdam Density Functional program package, ADF2013.01.<sup>41-43</sup> Geometry optimizations of  $\text{Pc}^{3-}$ ,  $\text{MgPc}^-$  and  $\text{MnPc}$  was performed using local density approximation (LDA) characterized by the Vosko-Willk-Nusair (VWN) parameterization,<sup>44</sup> as well as with general gradient approximation (GGA) in the form of OPBE<sup>45</sup> and with hybrid B3LYP\*<sup>46</sup> functional. Molecular orbitals were expanded in an uncontracted set of Slater type orbitals (STOs) of Triple-zeta quality with double polarization function (TZ2P) basis set.<sup>47,48</sup> All electrons were treated explicitly during the geometry optimizations. An auxiliary set of s, p, d, f, and g STOs was used to fit the molecular density and to represent the Coulomb and exchange potentials accurately for each SCF cycle. All calculations were spin-unrestricted. Geometries of all possible spin states (doublet, quartet and sextet) of  $\text{MnPc}$  were fully optimized. In addition, by imposing different occupation in the Kohn-Sham (KS) MOs, three intermediate spin states ( $^4E_g$ ,  $^4A_{2g}$ ,  $^4B_{2g}$ ) of  $\text{MnPc}$  are considered. For this purpose, energies and gradients were calculated also using BP86-D3,<sup>49-51</sup> S12g,<sup>52</sup> SSB-D,<sup>52</sup> M06-L,<sup>53</sup> PBE0<sup>54,55</sup> and TPSSH<sup>56</sup> DFAs. For all calculations

Becke grid of normal quality was used.<sup>57,58</sup> Harmonic frequencies were calculated in order to ascertain that all optimized structures are stationary points on the potential energy surfaces.

In order to quantify the JT effect in the cases where the ground state is orbitally degenerate, geometries and energies of the high symmetry (HS),  $D_{4h}$ , and low symmetry (LS),  $D_{2h}$ , nuclear arrangements should be known. The multideterminant electronic state of the HS configuration is represented with the average of configuration (AOC) SCF calculation,<sup>30</sup> where the degenerate orbitals are equally populated, leading to a homogenous distribution of electrons over the components of the degenerate irreducible representations (irrep). The AOC approach gives a proper geometry of the HS species. In order to get the energy of the HS molecular configuration, a single point calculation imposing the lower symmetry of the electron density is performed (second step). The last, straightforward step involves geometry optimization of the LS structures, yielding different LS geometries depending on the particular occupation of the originally degenerate KS MOs. The lowest energy structure is the minimum, while other LS structure is the saddle point. Their energy difference is the warping barrier,  $\Delta$ . The JT stabilization energy ( $E_{JT}$ ) is the difference in energies obtained in the second and the last step for the structures with the same electron distribution. The JT radius ( $R_{JT}$ ), describing a direction and magnitude of the JT distortion, is given by the length of the distortion vector between the HS and the LS minimum energy configurations.

The nature of metal-ligand bonding in  $\text{MgPc}^-$  and  $\text{MnPc}$  was analyzed with the aid of the EDA method<sup>59,60</sup> as implemented in ADF.<sup>42,43</sup> The interaction energy,  $E_{int}$ , between two fragments is decomposed into electrostatic, Pauli repulsion, and orbital interaction terms. The first term is the quasi-classical electrostatic interaction between the fragments; the second term is the repulsive Pauli interaction between occupied orbitals on the two fragments; the last term is the stabilizing interaction between the occupied MOs from one fragment with the unoccupied MOs of the other fragment and polarization in the same fragment. In attempt to clarify the origin of the JT distortion EDA was performed on the HS, as well as, on the LS distorted structures. In order to get  $E_{JT}$ , in addition to the changes in  $E_{int}$  when breaking the symmetry, it is necessary to consider changes in the preparation energies of the fragments,  $\Delta E_{prep}$  as well:

$$-E_{JT} = (E_{int}(LS) - E_{int}(HS)) + (E_{prep}(LS) - E_{prep}(HS)) = \Delta E_{int} + \Delta E_{prep} \quad (1)$$

The IDP,<sup>31-33,39,40</sup> method for the analysis of the multimode JT problem, is based on the fact that all the information about the vibronic coupling at the HS nuclear arrangement is also contained in the distorted LS minimum energy structure. The reference point for the method is the LS configuration, a true minimum on the potential energy surface, and the distortion is given as a superposition of all totally symmetric normal modes in the LS point group. The IDP is a reaction path starting from the HS geometry and ending in the LS minimum using the quadratic energy surface:

$$E_{JT} = \sum_i \frac{1}{2} K_i^{LS} [\vec{Q}_i^{LS}(HS)]^2 \quad (2)$$

where  $\vec{Q}_i^{LS}(HS)$  is the HS geometry expressed in terms of the LS vibrational modes, and  $K_i^{LS}$  are the harmonic force constants of the LS normal modes obtained from the DFT calculations. With this model it is possible to directly distinguish the contributions of the different normal modes to the JT distortion, the forces along either LS or HS normal modes at the HS point, as well as how these forces change along a relevant particular path of distortion.  $\vec{R}_{JT}$  is expressed in terms of either LS or HS normal modes:

$$\vec{R}_{JT} = \sum_i r_{JT,i}^{LS} \vec{Q}_i^{LS} = \sum_i r_{JT,i}^{HS} \vec{Q}_i^{HS} \quad (3)$$

where  $r_{JT,i}$  is the contribution of the displacements along the LS or HS normal coordinate to the  $\vec{R}_{JT}$ , or in other words the JT radius of the particular normal mode.

## Results and Discussion

In order to clarify the complicated electronic structure of MnPc, DFT calculations for its lowest lying electronic states were performed using various DFAs. Mn<sup>II</sup> in the square-planar environment has five electrons in the 3d shell, leading to the three possible spin states: low spin,  $S=1/2$ , intermediate spin,  $S=3/2$  and high spin,  $S=5/2$ . These three spin states produce five lowest lying electronic states, out of which three belong to the intermediate spin state, Table 1 and Figure 1. Other possible electronic states are at least 20 kcal mol<sup>-1</sup> higher in energy than the high spin state, and thus, is excluded from further consideration. Although previous experimental<sup>21-24,61</sup> and theoretical studies<sup>22,25,62-64</sup> have agreed that intermediate spin state is the ground state, the order of the close-lying quartet electronic states is still not clear. According to the different experimental techniques, the ground state is either assigned as  ${}^4E_g$ ,<sup>23,26,62-64</sup> or  ${}^4E_g$  and  ${}^4A_{2g}$  are equally possible<sup>21,22</sup>. Single-crystal magnetic study found  ${}^4A_{2g}$  as the electronic ground state.<sup>27</sup> Previous experimental study<sup>65</sup> revealed  ${}^4A_{2g}$  ground state into which the excited  ${}^4E_g$  term is mixed by spin-orbit coupling. Our DFT calculations revealed that regardless of the DFAs used, intermediate spin (1 on the Figure 1),  ${}^4E_g$ , is the ground state, Table 1.

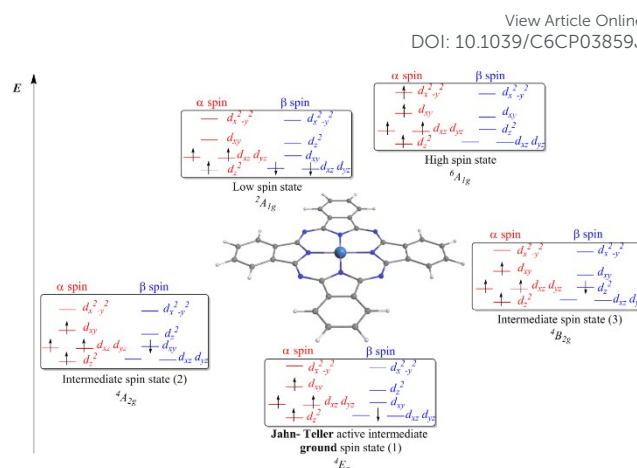


Figure 1. Qualitative energetics and electronic configurations for the five lowest lying electronic states of MnPc calculated with B3LYP\*.

It is worth to mention that GGAs and meta-GGA gave that  ${}^4E_g$  is more stable than  ${}^4A_{2g}$  (depicted in the Figure 1 as 2), and  ${}^4B_{2g}$  (3 on the Figure 1) for approximately 10 kcal mol<sup>-1</sup>. In the case of OPBE, a large energy difference between intermediate spin  ${}^4B_{2g}$  and  ${}^4A_{2g}$  states is obtained. The energy difference between  ${}^4E_g$  and  ${}^4A_{2g}$  calculated with hybrids, B3LYP\*, PBE0 and TPSSh, is smaller, Table 1. It is well-known fact that some GGAs such as OPBE, S12g and SSB-D, as well as M06-L, B3LYP\* and TPSSh are superior for the determination of energy difference between various spin states,<sup>46,66-70</sup> but since the three lowest electronic states belong to the same intermediate spin state, it should not be surprising that hybrid functionals perform better. B3LYP\* and TPSSh gave good relative spin state energetics, while PBE0 artificially stabilized the high spin state.

In summary, irrespective of the choice of DFAs  ${}^4E_g$  is the ground state. This degenerate electronic ground state is prone to the JT distortion, same as in the case of MgPc<sup>-</sup> and Pc<sup>3-</sup>. All three considered molecules in the electronic ground state have a single electron or a hole in a doubly degenerate HOMO, leading to  ${}^2E_g$  ( ${}^4E_g$  for MnPc) ground electronic state, in perfect square-planar nuclear configurations that belong to the  $D_{4h}$  point group. The symmetric direct product of the  $E_g$  electronic state transforms as  $A_{1g}+B_{1g}+B_{2g}$ , giving the symmetries of the JT active normal modes. These three vibrations in square-planar structures are depicted in Figure 2, using the vibrational energy distribution representation.<sup>71</sup>

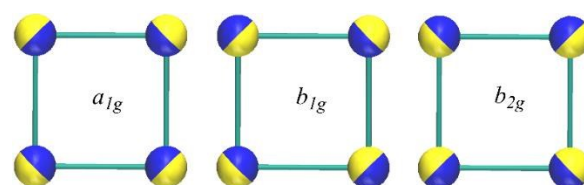


Figure 2. Schematic vibrational energy distribution representation of the  $a_{1g}$ ,  $b_{1g}$  and  $b_{2g}$  normal modes in  $D_{4h}$  point group. The different colors indicate the direction of the displacement vector.

Table 1. Energy differences (kcal mol<sup>-1</sup>) for the five lowest lying electronic states of MnPc calculated with different DFAs.

Electronic state		BP86-D3	OPBE	S12g	SSB-	M06-	B3LYP*	PBE0	TPSSh
Low spin	<sup>2</sup> A <sub>1g</sub>	24.25	17.4	17.3	32.49	16.51	16.92	22.4	15.76
Intermediate spin (1)	<sup>4</sup> E <sub>g</sub>	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
Intermediate spin (2)	<sup>4</sup> A <sub>2g</sub>	8.81	11.2	12.2	12.41	15.35	3.97	2.63	5.45
Intermediate spin (3)	<sup>4</sup> B <sub>2g</sub>	10.79	17.2	12.1	12.78	13.15	6.94	7.75	8.67
High spin	<sup>6</sup> A <sub>1g</sub>	25.20	15.4	19.9	14.66	12.94	13.31	4.59	16.33

Vibrations that belong to both  $B_{1g}$  and  $B_{2g}$  irreps in  $D_{4h}$  point group distort square-planar structure to a structure with lower  $D_{2h}$  symmetry, rhombus and rectangle, respectively. In the case of investigated molecules, the distortion is not obvious as in the simple JT active square-planar molecules because of a delocalized nature of the active normal modes, but it primarily occurs in the square labeled in Figure 3. Our calculations revealed that in all three cases,  $b_{1g}$  normal modes in  $D_{4h}$  point group lead to the minima, while  $b_{2g}$  ones guide the molecules to the transition states on the potential energy surfaces. As a consequence, <sup>2</sup>E<sub>g</sub> (<sup>4</sup>E<sub>g</sub>) ground electronic state splits into two non-degenerate electronic states, <sup>2</sup>B<sub>3g</sub> (<sup>4</sup>B<sub>3g</sub>) and <sup>2</sup>B<sub>2g</sub> (<sup>4</sup>B<sub>2g</sub>) in  $D_{2h}$  point group, resulting in the stabilization of the molecules.

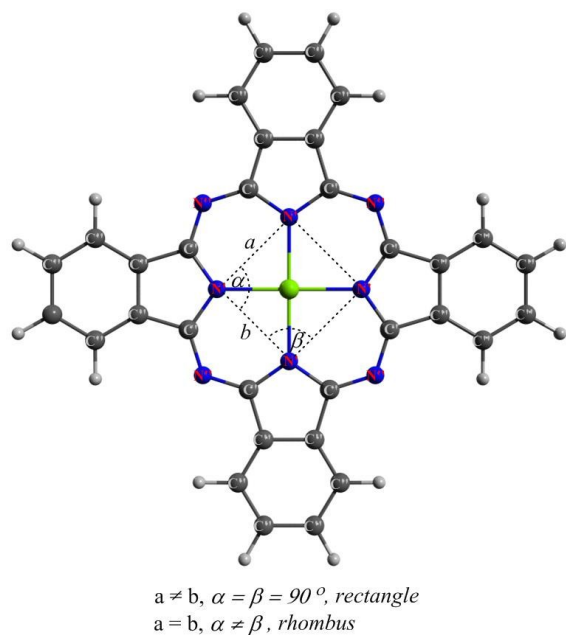


Figure 3. Schematic representation of the LS structures in investigated molecules. Nitrogen and carbon atoms are labelled as N', C', N'' and C''.

The JT parameters,  $E_{JT}$ ,  $\Delta$  and  $R_{JT}$ , for  $\text{Pc}^{3-}$ ,  $\text{MgPc}^-$  and  $\text{MnPc}$  were calculated by well-established DFT procedure<sup>30-36</sup> with LDA, OPBE and B3LYP\*, Table 2. The choice of DFA have been made from previous experience in determination of the JT parameters by DFT,<sup>30-36</sup> where LDA is shown to be the most accurate functional in comparison with other theoretical and/or experimental results. In this work obtained values do not depend significantly on a choice of DFAs, except in the case of B3LYP\* where somewhat higher values of the JT parameters were noticed for  $\text{Pc}^{3-}$  and  $\text{MgPc}^-$ , Table 2. Insertion of  $\text{Mg}^{\text{II}}$  in the phthalocyanine core leads to the higher JT stabilization energies, although overall distortion is smaller, Table 2. According to earlier DFT study,<sup>72</sup> the values of  $E_{JT}$  for minimum and transition state of  $\text{MgPc}^-$  were 406 and 187 cm<sup>-1</sup>, respectively, which is in very good agreement with our calculations, although the computation procedures differ.

Table 2. Results of the DFT calculations performed to analyze the JT effect in  $\text{Pc}^{3-}$ ,  $\text{MgPc}^-$  and  $\text{MnPc}$ ; the JT parameters  $E_{JT}$  and  $\Delta$  are given in cm<sup>-1</sup> and  $R_{JT}$  in (amu)<sup>1/2</sup>Å.

Molecule	Symmetry	LDA	OPBE	B3LYP*
$\text{Pc}^{3-}$	$E_{JT}, {}^2B_{2g}$	319	331	454
	$E_{JT}, {}^2B_{3g}$	141	146	253
	$E_{JT}(\text{IDP}), {}^2B_{2g}$	305	311	465
	$E_{JT}(\text{IDP}), {}^2B_{3g}$	142	148	214
	$\Delta$	178	185	201
	$R_{JT}, {}^2B_{2g}$	0.34	0.32	0.34
	$R_{JT}, {}^2B_{3g}$	0.21	0.26	0.20
$\text{MgPc}^-$	$E_{JT}, {}^2B_{2g}$	399	421	614
	$E_{JT}, {}^2B_{3g}$	181	194	273
	$E_{JT}(\text{IDP}), {}^2B_{2g}$	402	417	606
	$E_{JT}(\text{IDP}), {}^2B_{3g}$	191	204	277
	$\Delta$	218	227	341
	$R_{JT}, {}^2B_{2g}$	0.13	0.13	0.17
	$R_{JT}, {}^2B_{3g}$	0.15	0.14	0.17
$\text{MnPc}$	$E_{JT}, {}^4B_{2g}$	137	178	152
	$E_{JT}, {}^4B_{3g}$	13	25	27
	$E_{JT}(\text{IDP}), {}^4B_{2g}$	142	181	178
	$E_{JT}(\text{IDP}), {}^4B_{3g}$	20	31	34
	$\Delta$	124	153	125
	$R_{JT}, {}^4B_{2g}$	0.12	0.10	0.13
$R_{JT}, {}^4B_{3g}$	0.21	0.17	0.17	

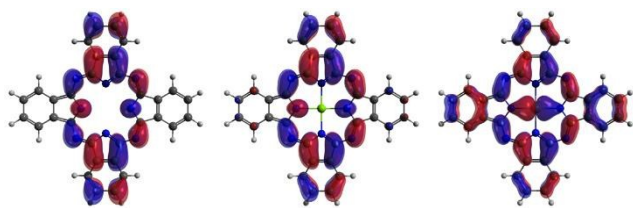


Figure 4. Schematic representation of one component of the doubly degenerate SOMOs in  $\text{Pc}^{3+}$ ,  $\text{MgPc}^-$  and  $\text{MnPc}$ .

The doubly degenerate SOMOs ( $D_{4h}$  point group), in the case of  $\text{Pc}^{3+}$  and  $\text{MgPc}^-$  are localized on the phthalocyanine ring, Figure 4. Contrary to the situation of  $\text{Pc}^{3+}$  and  $\text{MgPc}^-$ , in the case of  $\text{MnPc}$ , the delocalization of MOs occurs over the whole molecule, Figure 4. The participation of the  $\text{Mn}^{\text{II}}$  3d orbitals is not negligible, and at first glance, using MO analysis we can conclude that the  $\text{Mn}^{\text{II}}$  takes an important role in the JT distortion, although the quantitative picture remains secluded.

In order to clarify the origin of the JT distortion and determine whether the coordinated metal ion is the source of symmetry breaking, EDA was carried out for the HS and LS minimum structures of  $\text{MgPc}^-$  and  $\text{MnPc}$ . First, the investigated complexes were separated into two fragments which could, in a chemical way, be responsible for the JT phenomenon. The first fragment in both,  $\text{MgPc}^-$  and  $\text{MnPc}$ , is the divalent metal ion. While  $\text{Mg}^{\text{II}}$  is a closed-shell system,  $\text{Mn}^{\text{II}}$  is an open-shell system which could be the main reason and the source of the JT distortion in  $\text{MnPc}$ . The second fragment is  $\text{Pc}^{3+}$  for  $\text{MgPc}^-$  and  $\text{Pc}^{2+}$  for  $\text{MnPc}$ . All the energy components for  $\text{MnPc}$  and  $\text{MgPc}^-$  in the HS and LS configurations from EDA are given in the Supplementary information, Table S1 and Table S2.

The bonding analysis is summarized in Table 3, containing the leading components of  $E_{\text{JT}}$  from the EDA analysis, given as the relative energies between the HS and LS configurations. Relative preparation energy,  $\Delta E_{\text{prep}}$  is positive in the case of  $\text{MnPc}$ , stressing that closed-shell  $\text{Pc}^{2+}$  opposes the distortion, in contrast to the case of  $\text{MgPc}^-$ . In both cases, relative interaction energy,  $\Delta E_{\text{int}}$ , shows the stabilizing effect. The stabilization of  $E_{\text{int}}$  is more pronounced in the case of  $\text{MnPc}$ . Relative Pauli repulsion,  $\Delta E_{\text{Pauli}}$ , is opposing the distortion in the case of  $\text{MnPc}$ , while it shows only minor effect in  $\text{MgPc}^-$ .  $\Delta E_{\text{elstat}}$  is more stabilizing  $\text{MgPc}^-$ . The relative orbital interaction energy,  $\Delta E_{\text{orbint}}$ , has substantial stabilizing effect in the case of  $\text{MnPc}$ , because of the overlap between  $\text{Mn}^{\text{II}}$  3d orbitals and suitable ligand orbitals, Figure 4.  $\Delta E_{\text{orbint}}$  has negligible destabilizing effect in the case of  $\text{MgPc}^-$ . In summary, the JT distortion in  $\text{MnPc}$  arises because of stabilizing orbital interactions, while  $E_{\text{prep}}$  and  $E_{\text{Pauli}}$  are opposing the distortion. In  $\text{MgPc}^-$  the JT stabilization is due to the lowering of  $E_{\text{prep}}$  and  $E_{\text{elstat}}$ . The EDA analysis is not affected by the choice of DFA employed, Table 3. Small numerical variations arise mainly because of different geometries used in the calculations, as seen when EDA is performed with OPBE on LDA optimized geometries, Table 3.

Table 3. EDA analysis of  $\text{MnPc}$  and  $\text{MgPc}^-$  in the HS and LS configurations with LDA and OPBE; relative energies between HS and LS structures are given in  $\text{cm}^{-1}$ . DOI: 10.1039/C6CP03850A

	LDA	OPBE	OPBE/LDA*
MnPc			
$-E_{\text{JT}}$	-136	-178	-169
$\Delta E_{\text{prep}}$	176	103	181
$\Delta E_{\text{int}}$	-312	-281	-350
$\Delta E_{\text{Pauli}}$	155	39	144
$\Delta E_{\text{elstat}}$	-156	-60	-143
$\Delta E_{\text{orbint}}$	-311	-260	-351
MgPc			
$-E_{\text{JT}}$	-400	-421	-408
$\Delta E_{\text{prep}}$	-296	-282	-300
$\Delta E_{\text{int}}$	-104	-139	-108
$\Delta E_{\text{Pauli}}$	73	-8	78
$\Delta E_{\text{elstat}}$	-182	-165	-190
$\Delta E_{\text{orbint}}$	5	34	5

\*OPBE single point on LDA geometries

The distortion from the HS nuclear arrangement, due to the JT effect, towards the LS energy minimum conformation is a displacement on the 3N-6 potential energy surface. In the realistic situations, several JT active modes are responsible for the distortion, and it is not possible to know a priori the individual role of different normal modes in the observed JT induced properties. These molecules are, thus, typical examples of the multimode JT problem. In order to ensure further insight and determine the linear vibronic coupling constants in  $\text{Pc}^{3+}$ ,  $\text{MgPc}^-$  and  $\text{MnPc}$ , the forces at the HS point were calculated toward the distortion to the LS structures, Table 4. An analysis of the multimode JT distortion shows that, out of 28 totally symmetric normal modes in the LS minimum conformation, in the case of  $\text{Pc}^{3+}$  10 normal modes describe the distortion, Table 4. In the case of  $\text{MgPc}^-$  and  $\text{MnPc}$ , out of 28  $a_g$  modes, 11 vibrations are sufficient to completely characterize the distortion, Table 4. These normal modes contribute the most to the JT distortion ( $R_{\text{JT}}$ ), and to the total force at the HS point.

In the case of  $\text{Pc}^{3+}$  the distortion starts with the normal mode of  $1556 \text{ cm}^{-1}$ , localized in C'-N'' bonds, Table 4 and Figures 3, 5 and 6. The vibrations of  $1449 \text{ cm}^{-1}$  (mainly localized in benzene rings of  $\text{Pc}^{3+}$ , Figure 3 and Figure 6) and  $720 \text{ cm}^{-1}$  (C'-N'-C' bending where the opposite ones are in the same phase, Figure 3 and Figure 6) also play a role in the stabilization of the molecule, Table 4 and Figure 5. The contributions of these three normal modes to the total force decrease rapidly along the IDP path. Although the lowest frequency mode of  $118 \text{ cm}^{-1}$  does not have important contribution to the total force, it contributes the most to the overall distortion, Table 4 and Figure 5. In the second region of the IDP, this soft mode, N'N' asymmetric stretch (Figure 3 and Figure 6), leads molecule toward the global minimum, playing the main role concerning the JT radius.

Table 4. Analysis of the multimode JT effect in  $\text{Pc}^{3-}$ ,  $\text{MgPc}^-$  and  $\text{MnPc}$  at the  $D_{4h}$  nuclear configuration: the JT radii ( $r_{JT,i}$ , ( $\text{amu})^{1/2}\text{\AA}$ ), contribution of the most relevant  $D_{4h}$  normal modes to the distortion ( $c_i$ ), and the forces (linear vibronic coupling constants,  $F_i^{\text{HS}}$ ,  $\text{cm}^{-1}/\text{\AA}$ ) of the most relevant  $D_{4h}$  normal modes. Total force along all JT active  $b_{1g}$  modes is 19638  $\text{cm}^{-1}/\text{\AA}$ , 25297  $\text{cm}^{-1}/\text{\AA}$  and 13115  $\text{cm}^{-1}/\text{\AA}$  for  $\text{Pc}^{3-}$ ,  $\text{MgPc}^-$  and  $\text{MnPc}$ , respectively. The total  $r_{JT}$  and  $F^{\text{HS}}$  are vector sum.

$\text{Pc}^{3-}, D_{4h} \rightarrow D_{2h}$			
Freq., $\text{cm}^{-1}$	$r_{JT,i}$ , ( $\text{amu})^{1/2}\text{\AA}$	$c_i$	$F_i^{\text{HS}}$ , $\text{cm}^{-1}/\text{\AA}$
118	0.3121	0.8637	218
531	0.0308	0.0084	820
720	0.0769	0.0525	4641
765	0.0202	0.0036	1412
1089	0.0290	0.0075	2957
1166	0.0110	0.0011	1174
1271	0.0469	0.0196	7783
1449	0.0330	0.0097	7272
1556	0.0601	0.0320	15301
1574	0.0054	0.0003	1211
Total	0.3355	0.9984	19581
$\text{MgPc}^-, D_{4h} \rightarrow D_{2h}$			
Freq., $\text{cm}^{-1}$	$r_{JT,i}$ , ( $\text{amu})^{1/2}\text{\AA}$	$c_i$	$F_i^{\text{HS}}$ , $\text{cm}^{-1}/\text{\AA}$
179	0.0216	0.0269	209
560	0.0179	0.0184	391
758	0.0696	0.2793	4917
796	0.0339	0.0662	2462
1116	0.0285	0.0468	3179
1200	0.0257	0.0382	3562
1327	0.0200	0.0230	3353
1410	0.0110	0.0070	2428
1454	0.0405	0.0943	8927
1592	0.0630	0.2286	16757
1602	0.0532	0.1630	14415
Total	0.1312	0.9917	25271
$\text{MnPc}, D_{4h} \rightarrow D_{2h}$			
Freq., $\text{cm}^{-1}$	$r_{JT,i}$ , ( $\text{amu})^{1/2}\text{\AA}$	$c_i$	$F_i^{\text{HS}}$ , $\text{cm}^{-1}/\text{\AA}$
199	0.0839	0.4653	341
568	0.0249	0.0409	844
760	0.0580	0.2226	3932
805	0.0252	0.0420	1869
1126	0.0246	0.0400	3008
1194	0.0276	0.0502	4228
1331	0.0022	0.0003	654
1420	0.0209	0.0288	4464
1458	0.0285	0.0536	6238
1605	0.0210	0.0290	5752
1634	0.0197	0.0257	5716
Total	0.1229	0.9984	13105

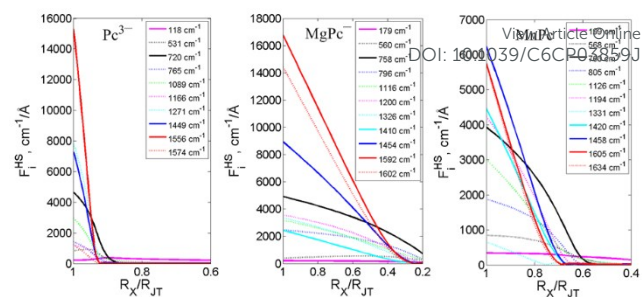


Figure 5. IDP analysis of the  $D_{4h} \rightarrow D_{2h}$  multimode JT distortion in  $\text{Pc}^{3-}$ ,  $\text{MgPc}^-$  and  $\text{MnPc}$ , respectively. Changes of the forces along the most important  $D_{4h}$  normal modes.

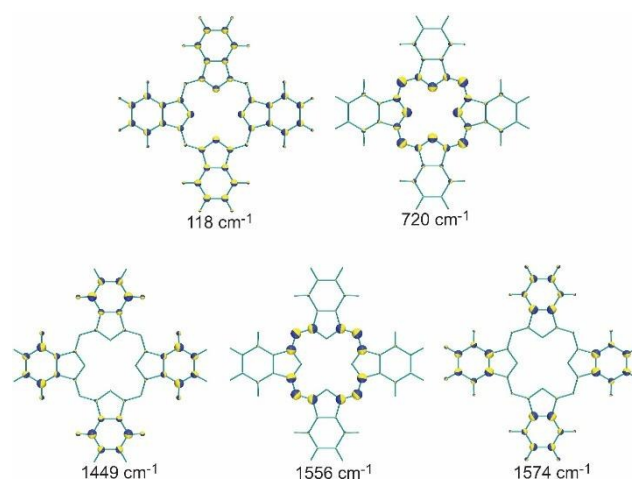


Figure 6. Schematic representation of the most important normal modes in  $\text{Pc}^{3-}$ . The size of vibrational motion on a nucleus is represented as sphere with the radius depending on the magnitude of the motion. The different colors indicate the direction of the motion.

Although coordination of  $\text{Pc}^{3-}$  to the magnesium divalent ion does not influence the doubly degenerate SOMO, Figure 4, the JT stabilization energy and the driving force are larger than in the case of  $\text{Pc}^{3-}$ , while the distortion is almost twice smaller, Tables 2 and 4. The reason behind this is in the significant participation of the harder modes in the JT distortion. However, the coordination to the metal ion makes the molecule more rigid, and thus producing smaller  $R_{JT}$ .

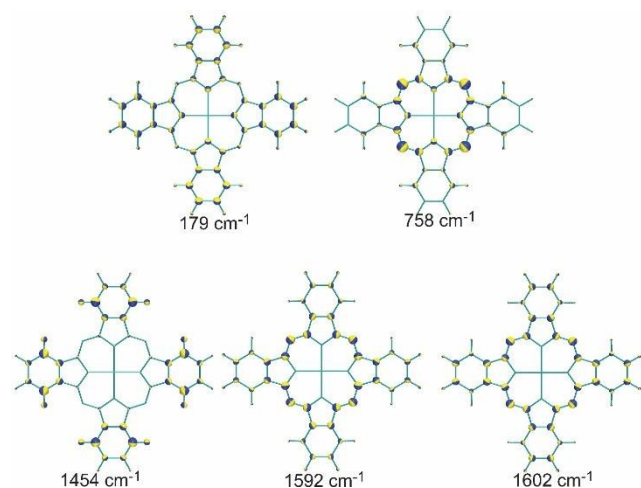


Figure 7. Schematic representation of the most important normal modes in  $\text{MgPc}^-$ . The size of vibrational motion on a nucleus is represented as sphere with the radius depending on the magnitude of the motion. The different colors indicate the direction of the motion.

The vibrations of 1602 and 1592  $\text{cm}^{-1}$  correspond to the normal modes localized in the C'-N" bonds and in benzene rings, Figures 3, 5 and 7. These two modes have the largest linear vibronic coupling constants, Table 4 and Figure 5, although the contribution of vibration of 1454  $\text{cm}^{-1}$  localized in benzene rings, Figure 7, is non-negligible, Table 4 and Figure 5. It is interesting to notice that in contrast to the potential energy surface of  $\text{Pc}^{3-}$ , the IDP analysis did not find the softest mode of 179  $\text{cm}^{-1}$  to contribute significantly to the JT distortion, Table 4 and Figure 5. In this case, 11 normal modes play a role in the overall distortion, while the most dominant ones are vibrations of 1602, 1592, 1454 and 758  $\text{cm}^{-1}$ , Table 4 and Figure 5. The vibration of 758  $\text{cm}^{-1}$  corroborates the normal mode of 720  $\text{cm}^{-1}$  in  $\text{Pc}^{3-}$ , Figures 6 and 7.

In order to make a comparison we refer to the work of Tóbiš et al.,<sup>72</sup> where the linear vibronic coupling constants of all the JT active modes are determined, using neutral  $D_{4h}$   $\text{MgPc}$  geometry, as the starting point. The contribution of the  $b_{1g}$  modes to the driving force is overall in a good agreement with the previously reported values,<sup>72</sup> Figure 8. The only difference is in the contribution of the totally symmetric normal modes distortion. Within the IDP model, the AOC geometry of  $\text{MgPc}^-$  is used. The neutral  $\text{MgPc}$  and charged  $\text{MgPc}^-$  obtained by AOC type calculations have different electronic structures, and different geometries, rationalizing the discrepancy. However, if we take the geometry of the neutral  $\text{MgPc}$  as the HS structure, the values are in agreement with Tóbiš et al.,<sup>72</sup> Figure 8, giving us the confidence in the obtained results, and showing the importance of the choice of HS geometry.

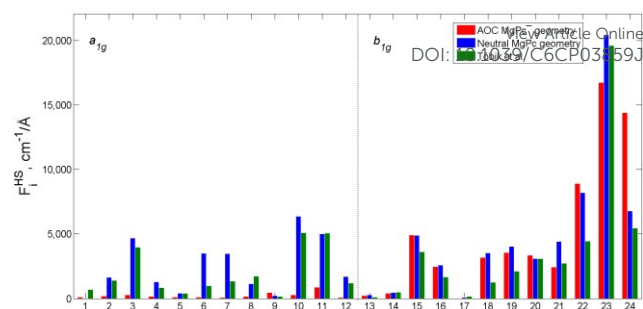


Figure 8. Comparison of the contributions to the  $F^{\text{HS}}$  of different  $D_{4h}$  normal modes in  $\text{MgPc}^-$  for different  $D_{4h}$  geometries (from AOC geometry optimization of  $\text{MgPc}^-$  and from neutral  $\text{MgPc}$ ) with those of Tóbiš et al.<sup>72</sup>

On the potential energy surface of  $\text{MnPc}$ , the modes of 1634, 1605 and 1458  $\text{cm}^{-1}$  afford the largest coupling constants, and hence stabilize the molecule, Table 4 and Figures 5 and 9, although the contribution of other  $b_{1g}$  vibrations cannot be neglected since the SOMO is delocalized over the whole system (Figure 4). As a consequence, and contrary to the previously investigated species, the initial force is obtained as a superposition of more normal modes, with almost the same contribution, Table 4 and Figure 5. Soft mode of 199  $\text{cm}^{-1}$  (Figure 9), corroborating the soft modes of 118 and 179  $\text{cm}^{-1}$  in  $\text{Pc}^{3-}$  and  $\text{MgPc}^-$ , respectively (Figures 6 and 7) becomes more important in the second region, allowing relaxation, and the potential energy surface is more flat.

To summarize, IDP model successfully explained which normal modes have the most important role in the stabilization of the systems and the overall distortion. In the case of  $\text{Pc}^{3-}$  and  $\text{MgPc}^-$ , hard modes are responsible for the stabilization.

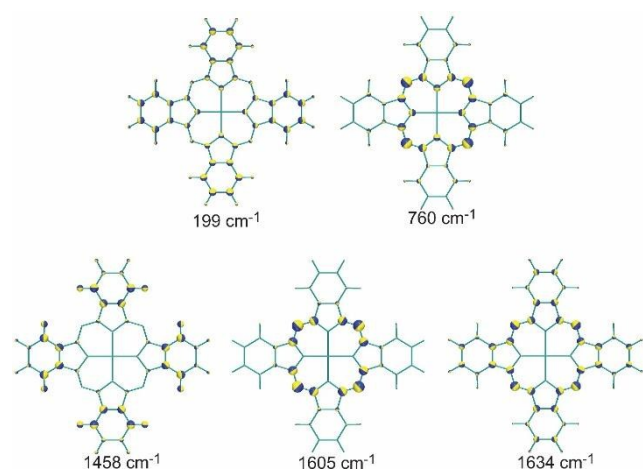


Figure 9. Schematic representation of the most important normal modes in  $\text{MnPc}$ . The size of vibrational motion on a nucleus is represented as sphere with the radius depending on the magnitude of the motion. The different colors indicate the direction of the motion.



The important difference between the multimode problems in these two molecules is that the  $\text{MgPc}^-$  is not relaxed toward the global minimum structure by the softest frequency mode. Because SOMO in  $\text{MnPc}$  is delocalized over the entire molecule, it is not surprising that eleven  $b_{1g}$  normal modes in the  $D_{4h}$  nuclear configuration are almost equally important to accurately describe the relaxation of the system. There are several normal modes relevant for the stabilization, which is in contrast to the situation in  $\text{Pc}^{3+}$  and  $\text{MgPc}^-$ .

## Conclusion

The discovery of the JT effect has become a source of inspiration for many researchers, not only as an adoption of new cognitions, but it affects many fundamental properties of molecules. In the framework of vibronic coupling theory it is possible to find rationalizations of different molecular phenomena. Since the electron doping of various metallophthalocyanines produces conductors from initial insulators, and also opens the road to the coupling of electronic states and nuclear motions, the proper determination of the JT distortion is an important prerequisite for the analysis of various properties of complex systems. Our calculations revealed that among different possible intermediate spin states,  $^4E_g$  is the ground state in  $\text{MnPc}$ , irrespective of level of theory employed, giving the rise to the vibronic coupling.

In order to understand the origin of the JT distortion, EDA analysis in  $\text{Pc}^{3+}$ ,  $\text{MgPc}^-$  and  $\text{MnPc}$  is presented. Considering  $\text{MnPc}$ , leading stabilizing contributions are based on the electron density of the  $\text{Mn}^{\text{II}}$  ion, in contrast to the  $\text{MgPc}^-$ . It is clear that the central metal ion presents the trigger for the JT distortion to occur over the whole system. The crucial effect in the case of  $\text{MgPc}^-$  is the preparation energy, acting in a stabilizing way. Since the preparation energy is completely located on the phthalocyanine ligand, the JT distortion occurs in  $\text{Pc}^{3+}$  core. To complete understanding of the JT phenomena in these similar systems, IDP model for the analysis of the multimode JT effect is successfully employed. The change of contribution of different vibrations to the JT distortion is obtained by expressing the distortion along the minimal energy path from HS to LS minimum structures. In the case of  $\text{Pc}^{3+}$  and  $\text{MgPc}^-$  only hard modes take the role in the stabilization. However, careful inspection revealed that softer modes become equally important along with the hard vibrations for the accurate description of the  $\text{MnPc}$  stabilization. It is important to highlight that obtained results indicate that the JT distortion is highly influenced by the coordination of phthalocyanine to the  $\text{Mn}^{\text{II}}$  ion, while  $\text{MgPc}^-$  complex ion possesses mainly ligand-based instability.

Different type of distortions and different nature of the symmetry breaking arise in these similar systems since different normal modes are responsible for the JT effect. This is of great importance, since neglecting nuclear displacements caused by an electronic structure would lead to the lack of explanation of many physical and chemical phenomena. This

is certainly significant for the rational design of new phthalocyanine materials with desired properties.

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