**Supporting Information for** 

## The Irony of Manganocene – An Interplay Between the Jahn-Teller Effect and Close Lying Electronic and Spin States

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#### Theoretical background and Computational details

All DFT calculations were performed with the Amsterdam Density Functional (ADF) suite of program.<sup>1,2</sup> MOs were expanded in an uncontracted set of Slater type orbitals (STOs) of triple- $\zeta$  quality (TZP)<sup>3</sup> and one set of polarization functions. An auxiliary set of s, p, d, f, and g STOs was used to fit the molecular density and to represent the Coulomb and exchange potentials accurately for each SCF cycle. Geometries were optimized with the QUILD program<sup>4</sup> using adapted delocalized coordinates<sup>5</sup> until the maximum gradient component was less than 10<sup>-4</sup> a.u. Energies and gradients were calculated using the OPBE level of theory.<sup>6,7</sup> Nature of stationary points is confirmed by calculating analytical Hessians.

If any nonlinear molecule is found in the electronically degenerate state, there exist a non-totally symmetric normal mode which can reduce the symmetry, remove the degeneracy and lower the energy. In many reallife Jahn-Teller problems, there is more than one normal mode that participates in the structural relaxation and this situation is referred to as a multimode problem. The non-totally symmetric normal mode will distort the geometry to the first subgroup in which at least one of its components belongs to the total symmetric irreducible representation (irrep.). That JT active normal mode may not be the only symmetry label from the high symmetry point group that becomes total symmetric in the new point group and the contributions from all these modes are successfully captured using IDP methodology. In this Manuscript, the high symmetry point groups are  $D_{5h}$  and  $D_{5d}$ , the JT active normal mode belongs to the  $E_1$ ' and  $E_{1g}$  irreps., and they distort the structure to the  $C_{2v}$  and  $C_{2h}$  point groups, respectively.

**Degenerate states** were treated in accordance with all our previous work regarding Jahn-Teller effect,<sup>8-11</sup> by optimizing the geometry with a high symmetry structural constraint and AOC electronic configuration (with  $E_2$ ' state of manganocene, that would mean  $(e_2')^3(a_1')^2(e_1'')$  electronic configuration, in which ADF occupies the degenerate  $e_2'$  orbitals with 0.5  $\beta$  electrons each). Using this structure, the subsequent single points have been performed with the electronic density relaxed to a low symmetry subgroup (for  $D_{5h}$  the first subgroup is  $C_{2v}$ :  $e_2' \rightarrow a_1 + b_1$ ;  $a_1' \rightarrow a_1$ ;  $e_1'' \rightarrow a_2 + b_2$ ), with the two possible resulting configurations:

 $(e_2')^3(a_1')^2(e_1'') \rightarrow (a_1)^2(b_2)^1(a_1)^2(a_2)(b_1)$  or  $(a_1)^1(b_2)^2(a_1)^2(a_2)(b_1)$ .

Detailed descriptions of IDP and Jahn-Teller effect are presented elsewhere.<sup>9-11</sup> **The essence of the IDP** is to express the distortion along a model minimal energy path, projecting the one nuclear configuration to the normal modes of the other. This allows to determine the presence and significance of all normal modes involved. Normal modes are labeled with  $Q_i$ , and  $E_{JT}$  represents energy difference between high symmetry and low symmetry structures, whereas  $R_{JT}$  is used to describe the corresponding geometrical distortion. Analytical frequencies were calculated with ADF2013, OPBE/TZP/integration 6 level of theory, on AOC electronic configurations in degenerate states. In  $D_{5h}$  geometry, since the symmetry of the degenerate electronic state is  $E'_2$  the JT active vibrations must belong to  $E'_1$  irreducible representation. For the distortion in manganocene and ferrocenyl cation from  $D_{5h} \rightarrow C_{2v}$  geometry, the projection of the JT distortion on the normal modes (Eq. 1) of both low symmetry (in eq. LS) and high symmetry (in eq. HS) is compared:

$$R_{JT} = \sum_{i} \omega_{i}^{LS(HS)} \cdot Q_{i}^{LS(HS)} \xrightarrow{\text{normalizing } \omega_{i}^{LS(HS)} \text{ to } 1} C_{i}^{LS(HS)} \text{ with } \sum_{i} (C_{i}^{LS(HS)})^{2} = 1$$
 Eq.1

S1

Coefficients  $\omega_i^{LS(HS)}$  give a contribution of certain normal mode to the JT distortion, and they can be expressed in normalized form as  $C_i^{LS(HS)}$ .  $E_i^{LS(HS)}$  and  $F_i^{LS(HS)}$  show contributions through the specific normal modes to the  $E_{JT}$  and force at high symmetry point.

The energy of the nuclear configuration  $E_x$ , relative to the energy of the reference low symmetry configuration, in harmonic approximation, is expressed as the sum of the energy contributions of all low symmetry totally symmetric normal coordinates ( $N_{a1}$ ):

$$E_{X} = \sum_{k=1}^{N_{a1}} E_{kX} = \frac{1}{2} \sum_{k=1}^{N_{a1}} w_{Xk}^{2} Q_{k}^{2} \lambda_{k}$$
 Eq.2

where  $\lambda_k$  are the eigenvalues of the Hessian from the DFT calculations in the low symmetry minimum energy conformation. In this framework, we can analyze the multimode JT problem by expressing the R<sub>JT</sub> as a superposition of all of the totally symmetric normal coordinates and directly obtaining the energy contributions of all of the normal modes to the total stabilization energy:

$$E_{JT} = \sum_{k=1}^{N_{a1}} E_{kJT} = \frac{1}{2} \sum_{k=1}^{N_{a1}} w_{kJT}^{2} Q_{k}^{2} \lambda_{k}$$
 Eq.3

The force along the normal mode  $Q_k$ ,  $F_{Xk}$ , which drives the nuclei along that coordinate to the minimum, at any point is defined as a derivative of the energy over the Cartesian coordinates.

$$\mathbf{\dot{F}}_{Xtot} = \sum_{k=1}^{N_{a1}} \mathbf{\dot{F}}_{Xk} = \frac{1}{2} \sum_{k=1}^{N_{a1}} w_{Xk} \lambda_k M^{1/2} \mathbf{\dot{O}}_k$$
Eq.4

In the high symmetry point this will give information about the main driving force for the JT distortion.

All EDA calculations were performed with OPBE/TZ2P in order to minimize the basis set superposition error.

**The magnetic behavior** of coupled, spatially separated, local spins is commonly modeled using phenomenological Heisenberg-Dirac Hamiltonian,<sup>12</sup> that reduces complicated quantum mechanical problem to a simplified description in terms of spin degrees of freedom only. For a system that consist of two metal (or radical) centers it can be written as:

 $\hat{H} = -J_{AB}\hat{S}_A \cdot \hat{S}_B$  where  $\hat{S}_A$  and  $\hat{S}_B$  are spin-operators associated with the spin-moments of unpaired electrons residing on spin-centers A and B. Only the total spin is physical observable, and in the case of two local spins, the possible total spins are given by Clebsch-Gordan Series:  $S_A + S_B$ ,  $S_A + S_B - 1$ , ...,  $|S_A - S_B|$ . The two spin-centers are described as ferromagnetically aligned when they produce the maximum total spin  $(S_A^{\uparrow}, S_B^{\uparrow})$ , and antiferromagnetically aligned when they produce minimum total spin  $(S_A^{\uparrow}, S_B^{\downarrow})$ . The  $J_{AB}$  is the magnetic coupling parameter, which measures the strength of isotropic exchange interaction (is positive for ferromagnetic and negative for antiferromagnetic alignment). Thus, by knowing  $J_{AB}$ , it is possible to qualitatively account for the observed magnetic properties of the system. Currently the standard method for determining  $J_{AB}$  is by mapping differences in calculated total energies from electronic structure calculations onto the spin-states of Heisenberg-Dirac Hamiltonian <sup>13</sup>

The problem arises from the fact that only the ferromagnetically coupled ( $S_{MAX} = S_A + S_B$ ) state can be properly described by one Slater determinant. This instantly leads to the conclusion that multideterminantal methodologies that are based on configuration interaction,<sup>14,15</sup> should be used. Unfortunately, such methodologies are usually too computationally demanding to study the large di- and poly nuclear TM complexes, or even the relatively small systems with many unpaired electrons are currently unfeasable.<sup>12</sup> Another drawback is the fact that these systems often possess considerable dynamical correlation, which makes the accurate calculations even more difficult.

Noodleman's suggestion<sup>16,17</sup> was the approach called the broken-symmetry (BS), that represent multideterminantal states with only one antiferromagnetically coupled Slater determinant. One of the artifacts that comes as a consequence of this is the appearance of spin density on sites A and B, although the real singlet state should have spin density equal to zero in any point.<sup>18,19</sup> The key step of the methodology is that orbitals are allowed to relax from the starting form under the action of the variational principle.<sup>12,20</sup> Thus, system is given the additional variational flexibility to lower its energy, and the ground state is formed variationally as a mixture of ferromagnetic state and singlet states generated by charge-transfer (ionic states).<sup>12,20</sup> Although this process is essentially similar to CI, the BS formalism does not have enough flexibility and it can only mix single determinant ferromagnetic and ionic states, and the real ground state, multideterminantal singlet, is not included in a final result. Qualitatively, BS method yields a correct charge density, but, as previously mentioned, there is a fictitious spin density.<sup>18,19</sup>



Scheme S1. Model for the manganocene dimer that was utilized to extract  $J_{AB}$  coupling constant.

We extracted  $J_{AB}$  by using the broken symmetry computational methodology that is s approximately valid over the entire coupling strength regime<sup>21</sup> (Eq. 4) and a dimer model shown on a Scheme S1.

$$J_{AB} = -\frac{E_{HS} - E_{BS}}{\left\langle S^2 \right\rangle_{HS}} - \left\langle S^2 \right\rangle_{BS}} = -\frac{388.8 cm^{-1}}{30.04 - 5.01} = -15.5 cm^{-1}$$
Eq.4

The coordinates for the utilized model are extracted from the X-ray structure of zigzag polymer.



Figure S1. Frontier molecular orbitals for  $MnCp_2$  in  $D_{5h}$  symmetry.

Distance(Å)	OPBI	E	Exp. <sup>22</sup>
Distance(A)	<sup>6</sup> A <sub>1</sub> ' (D <sub>5h</sub> )	${}^{2}A_{1}$ (C <sub>2v</sub> )	
Mn-Cp	2.06	1.69	2.05
Mn-C	2.39	2.08	2.38
C-C	1.42	1.43	1.43
С-Н	1.09	1.09	1.12

Table S1. Selected average bond lengths (Å) for OPBE energy-minimized MnCp<sub>2</sub> structure and comparison to available gas phase diffraction data at elevated temperatures.

## The EDA - results

As it can be noted from Table 1, with Mn(Cp)<sub>3</sub>, interaction between prepared Mn<sup>2+</sup> and 3Cp<sup>2-</sup> fragments is greater for LS, but it is more than compensated with the  $\Delta E_{prep}$ , specifically  $\Delta E_{valexc}$  and  $\Delta E_{cyc-cyc}$ . Since  $\Delta E_{valexc}$  is fairly constant for a given metal in the concrete oxidation state, only  $\Delta E_{cyc-cyc}$  remains for the analysis. So, we conclude that the energy needed to bring 3Cp<sup>-</sup> anions to a molecular geometry is much greater for more compact LS. As a conclusion we could state that unfavorable repulsion between the negative Cp<sup>-</sup> anions overrides the stronger Ligands-Metal interactions in low spin state.

Table 2 shows similar trends with the important difference that repulsion between the negative Cp- anions in much smaller now and in is not enough to override the factors that stabilize the LS state.

#### The IDP analysis - results

The results of IDP analysis for  $D_{5h} \rightarrow C_{2v}$  distortion are summarized in Table S2 (for decomposition in low symmetry normal modes), Table S3 (in high symmetry normal modes), and graphically presented in Fig. S2 and Fig. S3 respectively. For  $D_{5d} \rightarrow C_{2h}$  distortion results are summarized in Table S4 (in high symmetry normal modes).

		. Mangai	nocene				Ferocen	yl cation	
irrep	freq(cm <sup>-1</sup> )	$C_i^{LS}$	$E_i^{LS}(\text{cm}^{-1})$	$F_i^{LS}(mdyne)$	irrep	freq(cm <sup>-1</sup> )	$C_i^{LS}$	$E_i^{LS}(\text{cm}^{-1})$	$F_i^{LS}(mdyne)$
B2	-82.6	0	0	0	B2	-115.2	0	0	0
A2	45.7	0	0	0	A2	28.2	0	0	0
Al	136.7	0.6161	55.344	-0.0158	Al	154.4	0.5931	62.5643	-0.0155
AI D2	264.7	0.0086	2.9096	-0.0196	B2	216.5	0	0	0
B2 D1	208	0	0	0	AI D1	301.0	0	0.0199	-0.0065
	369.4	0	0	0		360	0	0	0
A1	429.9	0.2966	263,502	0.182	A1	444.9	0.3963	347.0618	0.1989
B1	477.4	0	0	0	B1	500.4	0	0	0
A1	581.5	0.0022	3.6517	0.0443	A1	550.5	0.0025	3.3276	-0.0191
B2	584	0	0	0	B1	568	0	0	0
A2	584.1	0	0	0	A2	576.4	0	0	0
B1	584.7	0	0	0	B2	584.6	0	0	0
A2	767.7	0	0	0	A1	703.1	0.0005	1.0205	-0.0139
B2	775	0	0	0	A2	800.5	0	0	0
BI	777.7	0	0	0	BI	807.1	0	0	0
	/84.9	0.0302	89.5/15	-0.10//	B2 D1	827.7	0	0	0
A2 D1	/89./	0	0	0	BI A 1	848.7	0 0002	0 0152	0 0100
	790.0	0 0011	3 3458	0 0189		849.1 852 7	0.0003	0.9155	-0.0109
B2	81/13	0.0011	0	-0.0189	R1	857.9	0	0	0
B1	818.8	Ő	Ő	0	B2	861.8	0	0	0
A1	827.6	0.0286	94.07	-0.1138	A1	878.3	0.0046	15.5735	-0.0412
A2	847.6	0	0	0	Al	899.6	0.0006	2.1261	-0.0136
B2	855.2	0	0	0	A2	912.3	0	0	0
A1	868.6	0.0102	37.091	-0.0184	B2	916	0	0	0
B1	874.2	0	0	0	B1	929.1	0	0	0
B1	994.8	0	0	0	B2	1010.2	0	0	0
A1	1000.2	0.0037	17.6183	0.0357	A2	1013.4	0	0	0
A2	1001.7	0	0	0	B1	1014.6	0	0	0
B2	1002.3	0	0	0	Al	1019	0.0014	6.4918	-0.0225
Bl	1041.4	0	0	0	Al	1037.6	0.0003	1.6519	-0.0146
AI	1043	0.001/	8.8368	0.0321	BI	1055.1	0	0	0
A2 D2	1051.5	0	0	0	A2 D2	1001.7	0	0	0
	1055.8	0 0004	2 179	0 0355	D2 A 1	10/5./	0	0 0111	0 0016
R1	1121 1	0.0004	2.179	-0.0355	R1	1131.5	0	0.0111	-0.0010
A2	1228.6	Ő	Ő	0	A2	1240 1	0	0	0
B2	1229.1	Õ	Ő	Ő	B2	1241.2	Ő	Ő	Ő
B1	1362.3	0	0	0	B1	1364.3	Õ	0	0
A1	1374.6	0.0001	0.7723	-0.01	A2	1377.9	0	0	0
A2	1380.4	0	0	0	A1	1383.6	0	0.0512	-0.0033
B2	1389.4	0	0	0	B2	1397.5	0	0	0
A1	1413.5	0.0005	4.9981	0.0655	B2	1426.5	0	0	0
B1	1414.7	0	0	0	Al	1432.2	0.0004	3.7575	-0.0576
B2	1424.1	0	0	0	B1	1433	0	0	0
A2 D1	1426.7	0	0	0	A2	1433.1	0	0	0
BI	3167.5	0	0 2706	0 0228	AI D1	3193.7	0	0.0364	-0.0054
A1 A2	3108.5	0	0.3706	0.0328	B1 A2	3197.7	0	0	0
A2 B2	3175.4	0	0	0	A2 R2	3202.8	0	0	0
B1	3189	0	0	0	B1	3215	0	0	0
A1	3189 5	0	0 139	0 0047	A1	3215	0	0 0745	0 0088
A2	3195.2	Ő	0	0.0047	A2	32163	0	0	0
B2	3195.4	Ő	Ő	Ő	B2	3217	Ő	ŏ	ő
A1	3203.1	0	0.1232	0.0188	B1	3229.2	Õ	Õ	0
B1	3205.5	0	0	0	A1	3229.9	0	0.0001	-0.0022
Rrffa	mu) 1/2. Angst	=0.5694	Errfe	m <sup>-1</sup> )=584 5231		R <sub>17</sub> =0 5463	;	$E_{rr}(cm^{-1})=444$	4.6834
11((0		., 0.0071	D11(C			1.51 0.0103		-11(**** ) ++	

Table S2. Contributions of all low symmetry vibrations to the JT distortion  $(C_i^{LS})^2$ ,  $E_{JT}$  and force at high symmetry point.



Figure S2. IDP analysis of low symmetry vibrations for both MnCp<sub>2</sub> and [FeCp<sub>2</sub>]<sup>+</sup>.

Table S3. Contributions of all high symmetry vibrations to the JT distortion  $(C_i^{HS})^2$ ,  $E_{JT}$  and force at high symmetry point.

	Manga	nocene			Feroceny	l cation	
irrep	freq(cm <sup>-1</sup> )	$C_i^{HS}$	F <sup>HS</sup> (mdyne)	irrep	freq(cm <sup>-1</sup> )	$C_i^{HS}$	F <sup>HS</sup> (mdyne)
AAA1	38.9	0	0	AAA1	33.5	0	0
EE1:1	148.2	0	0	EE1:1	162.3	0	0
EE1:2	148.2	0.6549	-0.0099	EE1:2	162.3	0.5780	0.0148
AA1	298	0.0378	0.0244	AA1	304.8	0	-0.0029
EEE1:1	377.6	0	0	EEE1:1	369.5	0	0
EEE1:2	377.6	0	0	EEE1:2	369.5	0	0
AAA2	482.3	0	0	EE1:1	461.2	0	0
EE1:1	503.9	0	-0.0569	EE1:2	461.2	0.3830	-0.2016
EE1:2	503.9	0.2543	-0.1958	AAA2	503.6	0	0
EEE2:1	614	0	0	EEE2:1	592.6	0	0
EEE2:2	614	0	0	EEE2:2	592.6	0	0
EE2:1	626.5	Õ	Õ	EE2:1	610	Ő	Ő
EE2:2	626.5	0.0080	0.0572	EE2:2	610	0.0017	-0.0006
EEE1.1	786.2	0	0	EEE2·1	804.4	0	0
EEE1.2	786.2	Ő	Ő	EEE2:2	804.4	Ő	Ő
EEE2·1	793.2	Ő	Ő	EE2·1	831.3	0.0003	0.0037
EEE2.2	793.2	Ő	Ő	EE2:2	831.3	0.0005	0.0057
	805.1	Ő	0 0	A A 1	852.5	0.0005	-0.0008
ΔΔ1	81/ 9	0.0004	0.0019	EFE1.1	854.5	0.0005	0.0000
EE2·1	823.7	0.0004	0.0017	EEE1.1 FFF1.2	854.5	0	0
EE2.1 FF2.2	823.7 823.7	0.0280	0 1160		856.8	0	0
EE1.1	8267	0.0200	0.1105	EE1.1	891.2	0	0
EE1.1 EE1.2	820.7	0 0045	0.0350	EE1.1 EE1.2	881.2	0 0043	0 0406
EE1.2 EEE2.1	820.7	0.0043	0.0350	EE1.2 EEE2.1	024.6	0.0043	0.0400
EEE2.1	805.0	0	0	EEE2.1	924.0	0	0
EEE2.2	803.0	0	0	EEE2.2	924.0	0	0 0025
EE2:1	880.4	0 0044	0	EE2:1	932.5	0	0.0035
EEZ:Z	880.4	0.0044	-0.0077	EE212	932.5	0	0
EEEI:I	1002.1	0	0	EEEI:I	1016.3	0	0
EEEI:2	1002.1	0 0024	0 0217	EEEI:2	1010.5	0 0018	0 02(2
EEI:I	1012.1	0.0034	0.0317	EEI:I	1022	0.0018	0.0262
EEI:2	1012.1	0	0	EET:2	1022	0	0
EEE2:1	1048.6	0	0	EEE2:1	1059.5	0	0
EEE2:2	1048.6	0	0 0212	EEE2:2	1059.5	0	0
EE2:1	1056	0.0031	0.0313	EE2:1	1072.5	0	0 00 42
EE2:2	1056	0	0	EE2:2	10/2.5	0.0001	-0.0043
AAA2	1126.5	0	0	AAI	1134.2	0.0002	0.0026
AAI	1129.2	0	0.0416	AAA2	1134.6	0	0
AAAI	1232.2	0	0	AAAI	1242	0	0
AA2	1233	0	0	AA2	1243.2	0	0.0001
EEE2:1	1388.7	0	0	EEE2:1	1381.9	0	0
EEE2:2	1388.7	0	0	EEE2:2	1381.9	0	0
EE2:1	1405.4	0	0	EE2:1	1407.6	0	-0.0156
EE2:2	1405.4	0.0002	-0.0285	EE2:2	1407.6	0	0
EEEI:I	1424	0	0	EEI:I	1433.1	0	0
EEE1:2	1424	0	0	EE1:2	1433.1	0.0005	-0.0549
EE1:1	1425.9	0	0	EEE1:1	1435.1	0	0
EE1:2	1425.9	0.0010	-0.0632	EEE1:2	1435.1	0	0
EEE2:1	3171.2	0	0	EEE2:1	3199.4	0	0
EEE2:2	3171.2	0	0	EEE2:2	3199.4	0	0
EE2:1	3172.2	0	-0.0318	EE2:1	3201.1	0	0
EE2:2	3172.2	0	0	EE2:2	3201.1	0	-0.0046
EEE1:1	3188.4	0	0	EEE1:1	3214.4	0	0
EEE1:2	3188.4	0	0	EEE1:2	3214.4	0	0
EE1:1	3189.1	0	0	EE1:1	3215.5	0	0
EE1:2	3189.1	0	-0.0170	EE1:2	3215.5	0	-0.0100
AAA2	3201.9	0	0	AAA2	3227.6	0	0
AA1	3202.8	0	0.0144	AA1	3228.3	0	0.0004



Figure S3. IDP analysis of the high symmetry vibrations in MnCp<sub>2</sub>.

	Ferocenyl cation							
freq	(cm <sup>-1</sup> )	irrep	$C_i^{HS}$	$F_i^{HS}(mdyne)$	freq(cm <sup>-1</sup> )	irrep	$C_i^{HS}$	$F_i^{HS}(mdyne)$
12.3	3	A1.u	0	0	-22.3	A1.u	0	0
163	.1	E1.u:1	0	0	151.1	E1.u:1	0	0
163	.1	E1.u:2	0	0	151.1	E1.u:2	0	0
309	.2	A1.g	0.0152	0.011	300.3	A1.g	0.0586	0.0172
378	.4	E1.g:1	0.9643	0.1122	389	E1.g:1	0.8260	0.1096
378	.4	E1.g:2	0	0	389	E1.g:2	0	0.021
452	.1	E1.u:1	0	0	477.7	A2.u	0	0
452	1	E1.u:2	0	0	478.5	E1.u:1	0	0
507		A2 11	0	Ő	478 5	E1 u:2	0	Õ
589	.7	E2.u:1	0	Õ	607.3	E2.u:1	0	Õ
589	.7	E2.u:2	0	0	607.3	E2.u:2	0	Õ
613	4	E2 g 1	Õ	Ő	630.2	E2 g 1	0 0184	0.0601
613	4	F2 g.2	0.0005	0.0081	630.2	E2.g.1	0	0
802	5	E2.g.2 E2 u·1	0.0005	0.0001	788 /	EL g.1	0.019/	0.0615
802	5	E2.u.1 E2.u.2	0	0	788.4	E1.g.1	0.0174	0.0015
802. 922	5	E2.u.2 E2.a:1	0	0 0022	702.2	E1.g.2	0	0
033	.5	E2.g.1	0	0.0022	792.3	E2.u.1	0	0
055	.5	E2.g.2	0	0	192.5	E2.u.2	0	0
851	.1	AI.g	0	0.0074	802.8	AZ.U	0	0
854	.2	E1.g:1	0.0146	0.0599	812.7	Al.g	0.0005	-0.0011
854	.2	E1.g:2	0	0.0011	823.9	E2.g:1	0.0527	-0.1204
856	.5	A2.u	0	0	823.9	E2.g:2	0	0
880	.8	E1.u:1	0	0	824	E1.u:1	0	0
880	.8	E1.u:2	0	0	824	E1.u:2	0	0
927		E2.g:1	0	-0.0038	867.4	E2.u:1	0	0
927		E2.g:2	0	0	867.4	E2.u:2	0	0
927	.9	E2.u:1	0	0	876.6	E2.g:1	0.0093	-0.0009
927	.9	E2.u:2	0	0	876.6	E2.g:2	0	0
101	7.3	E1.g:1	0.0039	-0.0406	1005.2	E1.g:1	0.0064	-0.0406
101	7.3	E1.g:2	0	0	1005.2	E1.g:2	0	0
102	0.9	E1.u:1	0	0	1010	E1.u:1	0	0
102	0.9	E1.u:2	0	0	1010	E1.u:2	0	0
106	2.6	E2.u:1	0	0	1051.4	E2.u:1	0	0
106	2.6	E2.u:2	0	0	1051.4	E2.u:2	0	0
107	0.1	E2.g:1	0	0	1055.2	E2.g:1	0	0
107	0.1	E2.g:2	0	-0.0023	1055.2	E2.g:2	0.0061	-0.0382
113	3.8	Al.g	0.0001	0.0117	1128	A2.u	0	0
113	5.1	A2.u	0	0	1129.6	A1.g	0.0002	-0.0202
124	19	A2.9	0	-0.0001	1232.5	A2.9	0	0.0001
124	23	A1 u	Õ	0	1232.8	A1 11	Ő	0
138	82	E2 u:1	Ő	Ő	1397.9	E2 u:1	Ő	0
138	8.2	E2 u:2	Õ	Ő	1397.9	E2 u:2	Ő	Ő
140	1.2	E2.u.2 E2 $\alpha$ ·1	0	0.0070	1300 /	E2.u.2 E2 $\alpha$ ·1	0.0003	-0.0232
140	1.2	$E_{2.g.1}$	0	0.0070	1300 /	E2.5.1	0.0005	0.0252
140	1.2 2	E2.g.2	0	0	1399.4	E2.g.2	0	0
143	2	E1.u.1	0	0	1424.2	E1.u.1	0	0
143	2 5 6	E1.u.2 E1 ~·1	0	0	1424.2	E1.u.2	0	0
145	5.0	E1.g.1	0 0012	0 0720	1427.7	E1.g.1	0 0015	0
143	5.0	E1.g:2	0.0013	0.0728	1427.7	E1.g:2	0.0015	-0.0680
320	0.7	E2.UT	0	0	31/2.9	E2.UT	0	0
320	0.7	E2.u:2	0	U	31/2.9	E2.u:2	0	U 0.0250
320	1.5	E2.g:1	0	0	3173.1	E2.g:1	0	0.0358
320	1.5	E2.g:2	0	0.0022	3173.1	E2.g:2	0	0
321	5.2	E1.g:1	0	0	3189.5	E1.g:1	0	0
321	5.2	E1.g:2	0	0.0119	3189.5	E1.g:2	0	0.0130
321	6.1	E1.u:1	0	0	3190.1	E1.u:1	0	0
321	6.1	E1.u:2	0	0	3190.1	E1.u:2	0	0
322	8.4	A2.u	0	0	3203	A2.u	0	0
222	87	Δ1 σ	0	-0.0009	3203.4	Al σ	0	-0.0089

Table S4. Contributions of all high symmetry vibrations to the JT distortion  $(C_i^{HS})^2$ ,  $E_{JT}$  and force at high symmetry point (D5d).

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